#### **THEOREM 5-9**

Section 5.4

If two sides of a triangle are not congruent, then the larger angle lies opposite the longer side.

PROOF: SEE EXERCISE 13.

If... b > a

C A

Then...  $m \angle B > m \angle A$ 

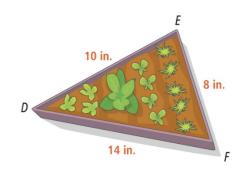
C

To support a triangular piece of a float, a brace is placed at the largest angle and a guide wire is placed at the smallest angle.

Which angle is the largest? 
Which angle is the smallest? 
SOLUTION

Lucas sketched a diagram for a garden box.

List the angles from least to greatest.



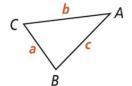
### **Converse of Theorem 5-9**

If two angles of a triangle are not congruent, then the longer side lies opposite the larger angle.

PROOF: SEE EXAMPLE 3.

If...  $m \angle B > m \angle A$ 

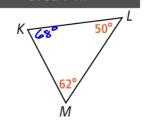
Then... b > a



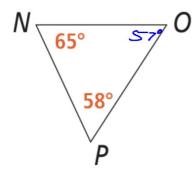
Which side of  $\triangle \mathit{KLM}$  is the longest?



SOLUTION



List the sides of triangles NOP from least to greatest.

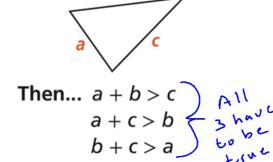


NP, NO, OP

# **Triangle Inequality Theorem**

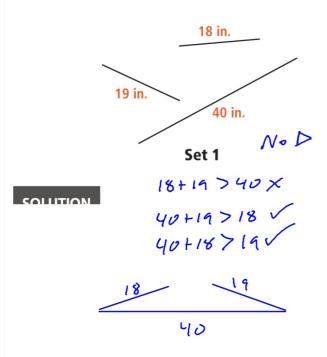
The sum of the lengths of any two sides of a triangle is greater than the length of the third side.

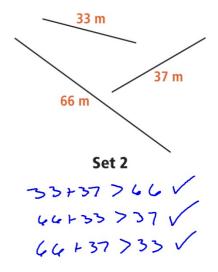
PROOF: SEE EXERCISE 14.



If...

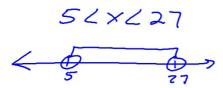
#### A. Which of the following sets of segments could be the sides of a triangle?

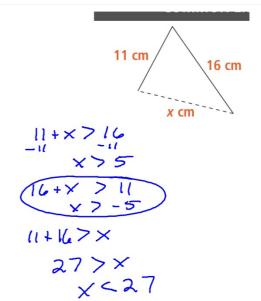




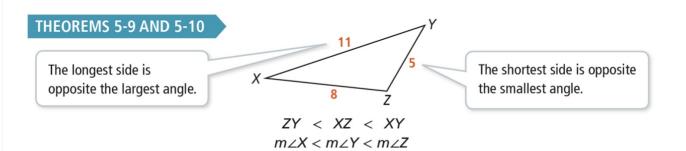
B. A triangle has sides that measure 11 cm and 16 cm. What are the possible lengths of the third side?







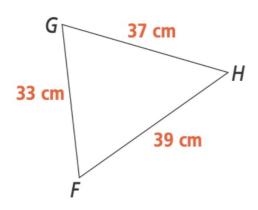
### **Inequalities in One Triangle**



#### **THEOREM 5-11** Triangle Inequality Theorem

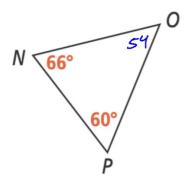
The sum of the lengths of any two sides is greater 5+8>11 than the length of the third side. 5+11>8 8+11>5

## Identify the angles of $\triangle FGH$ . SEE EXAMPLE 2.



- 18. Which angle is the smallest?
- 19. Which angle is the largest?

Identify the sides of  $\triangle NOP$ . SEE EXAMPLES 3 AND 4.



- **20.** Which side is the longest?  $\overline{OP}$
- 21. Which side is the shortest? NP

# Determine whether the side lengths could form a triangle. SEE EXAMPLE 5.

22. 13, 15, 9
$$13+15>9$$

$$13+15>9$$

$$15+1>13$$
23. 8, 15, 7
$$15+7>8$$

$$8+7>15$$
24. 35, 20, 11
$$35+20>11$$

$$20+11>35$$

$$05+32>40$$
32 +40>65 Yes
$$65+40>32$$

# Given two sides of a triangle, determine the range of possible lengths of the third side. SEE EXAMPLE 5.

26. 10 in. and 12 in.  $\frac{10+12>\times}{10+\times}$   $\frac{22>\times}{10+\times}$   $\frac{22>\times}{10+\times}$   $\frac{22\times}{10+\times}$   $\frac{22\times}$ 

28. 200 m and 300 m 200+300>x 500>x 1002x2500 x 200+>300 x 200+>300 x 200

29. 90 km and 150 km

60 < x < 240